

## Numerical Problems (Heritability & Genetic Gain)

1. The inbred lines of wheat are crossed. In the F<sub>1</sub> the variance in wheat yield is 1.5, the F<sub>1</sub> is selfed, in the F<sub>2</sub> the variance in wheat yield is 6.5. Estimate the H in broad sense of wheat yield in the experiment.

Solution:

Given,

Variance in F<sub>1</sub> is due to environment (V<sub>e</sub>) = 1.5

Phenotypic variance in F<sub>2</sub> (V<sub>p</sub>) = 6.5

$$\text{Heritability in broad sense (H)} = \frac{V_g}{V_p}$$

$$V_p = V_g + V_e$$

$$6.5 = V_g + 1.5$$

$$V_g = 5$$

$$\text{Heritability in broad sense (H)} = \frac{V_g}{V_p}$$

$$= \frac{5}{6.5}$$

$$= 0.76923$$

2. With the help of following data, calculate H and interpret the result.

SV	DF	SS	MSS
Genotype	48	419.4	10.8
Replication	2	0.08	0.04
Error	96	12.3	0.13

Solution:

$$\text{Heritability (H)} = \frac{V_g}{V_p}$$

$$V_g = \frac{\text{MSS due to genotype} - \text{MSS due to error}}{R}$$

$$V_g = \frac{10.8 - 0.13}{3}$$

$$= 3.5566$$

$$V_p = V_g + V_e$$

$$V_p = 3.5566 + 0.13$$

$$V_p = 3.6866$$

$$\text{Heritability (H)} = \frac{V_g}{V_p}$$

$$= \frac{3.5566}{3.6866}$$

$$= 0.96474$$

3. Calculate the H from the following information.

Population	Variance
P <sub>1</sub>	11
P <sub>2</sub>	10.32
F <sub>1</sub>	5.23
F <sub>2</sub>	90.35
BC <sub>1</sub>	47.35
BC <sub>2</sub>	54.29

Solution:

$$\text{Heritability (H)} = \frac{V_g}{V_p}$$

$$V_p = V_g + V_e$$

$$V_p = \text{Variance in F}_2 = 90.35$$

$$\begin{aligned} V_e &= \frac{P_1 + P_2 + F_1}{3} \\ &= \frac{11 + 10.32 + 5.23}{3} \\ &= 8.85 \end{aligned}$$

$$V_p = V_g + V_e$$

$$V_g = 90.35 - 8.85$$

$$= 81.5$$

$$\begin{aligned} \text{Heritability (H)} &= \frac{Vg}{Vp} \\ &= \frac{81.5}{90.35} \\ &= 0.90204 \end{aligned}$$

4. Estimate H through parent offspring regression method from the following available data:

Mid parent value(X)	Individual offspring (y)
20	25
18	21
25	20
17	20
21	26
22	25

Solution:

Mid parent value(X)	Individual Offspring(Y)	XY	$\sum X^2$
20	25	500	400
18	21	378	324
25	20	500	625
17	20	340	289
21	26	546	441
22	25	550	484
$\sum X = 123$	$\sum Y = 137$	$\sum XY = 2814$	$\sum X^2 = 2563$

$$b = \frac{\sum XY - \frac{\sum X \sum Y}{N}}{\sum X^2 - \frac{(\sum X)^2}{N}}$$

$$= \frac{2814 - \frac{123 \cdot 137}{6}}{2563 - \frac{15129}{6}}$$

$$= \frac{2814 - 2808.5}{2563 - 2521.5}$$

$$= \frac{5.5}{41.5}$$

$$= 0.1325$$

H = b (if mid-parents given)

H = 2b (if single parent value given)

**Question:**

- 1. For a quantity trait in a random population, mean is 100 and the variance is 240. The narrow sense heritability is 0.5. What is the expected mean of the next generation, if the top 10 % plants are used as parents.**

Solution:

$$\text{Mean of base population (X}_o\text{)} = 100$$

$$\text{Variance (V}_a\text{)} = 240$$

$$\text{Narrow sense heritability (h}^2\text{)} = 0.5$$

$$\text{Mean of the progeny (X}_p\text{)} = ?$$

$$\text{Selection intensity} = 10 \%$$

We know that,

$$R = X_p - X_o$$

And,

$$R = k \cdot h^2 \cdot \sigma_p$$

$$= 1.76 \cdot 0.5 \cdot 15.5$$

$$= 13.64$$

$\begin{aligned}\sigma_p &= \sqrt{V_a} \\ &= 15.5\end{aligned}$
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$$R = X_p - X_o$$

$$X_p = 13.64 + 100$$

$$= 113.64$$

2. In the same population above, if the breeder wants the next generation to have a mean is at least 120, what population of the top plants should be used for breeding?

Solution:

Mean of the progeny ( $X_p$ ) = 120

$K = ?$

We know,

$R = X_p - X_o$

= 120 - 100

= 20

$R = K \cdot h^2 \sigma_p$

$K = \frac{R}{h^2 \sigma_p}$

$\sigma_p = \sqrt{V_a}$ = 15.5
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= 2.58

So, selection intensity = near 1 %

Selection intensity %	Value of K
1	2.64
2	2.42
5	2.06
10	1.76
20	1.4

3. For a quantitative trait in a RPM, the mean is 100 and the variance is 240. The regression of the offspring on mid parent value is 0.25. Truncation selection is practiced with a selection differential of 32. What is the expected mean in the next generation?

Solution:

$$\text{Mean of base population } (X_o) = 100$$

$$b = h^2 = 0.25$$

$$\text{Selection differential } (S) = 32$$

$$\text{Expected mean in next gen. } (X_p) = ?$$

$$R = Sh^2$$

$$= 32 * 0.25$$

$$= 8$$

$$R = X_p - X_o$$

$$X_p = 8 + 100$$

$$= 108$$



4. The mean days to maturity and variance are 120 and 144 respectively. A plant breeder selected the top 5% plants from base population and found mean days to maturity 110 in the next generation. Find the genetic gain and the heritability of the trait.

Solution:

$$\text{Mean days to maturity } (X_o) = 120$$

$$\text{Variance } (V_a) = 144$$

$$\text{Selection intensity} = 5\%$$

$$\text{Value of K at 5\% selection intensity} = 2.06$$

$$\text{Mean days to maturity in next gen. } (X_p) = 110$$

$$\text{Genetic gain } (R) = ?$$

$$\text{Heritability } (h^2) = ?$$

$$R = X_p - X_o$$

$$= 110 - 120$$

$$= -10$$

(-ve sign indicated it is the condition of genetic gain. That means the variety matures 10 days earlier)

Now,

$$R = K \cdot h^2 \cdot \sigma_p$$

$$h^2 = \frac{R}{K \sigma_p}$$

$$= \frac{10}{2.06 \cdot 12}$$

$$= 0.40$$

Selection intensity %	Value of K
1	2.64
2	2.42
5	2.06
10	1.76
20	1.4

$$\sigma_p = \sqrt{V_a}$$

$$= 12$$